

Relative Pairwise Ranking: A normalization-free ordinal ranking approach for multi-criteria decision-making

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