



Tri-objective parallel machine with job splitting and sequence dependent setup times using differential evolution and particle swarm optimization

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